

Sensor-Utility-Network (SUN) Method for Estimating Occupancy in Buildings

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Joint Work With:

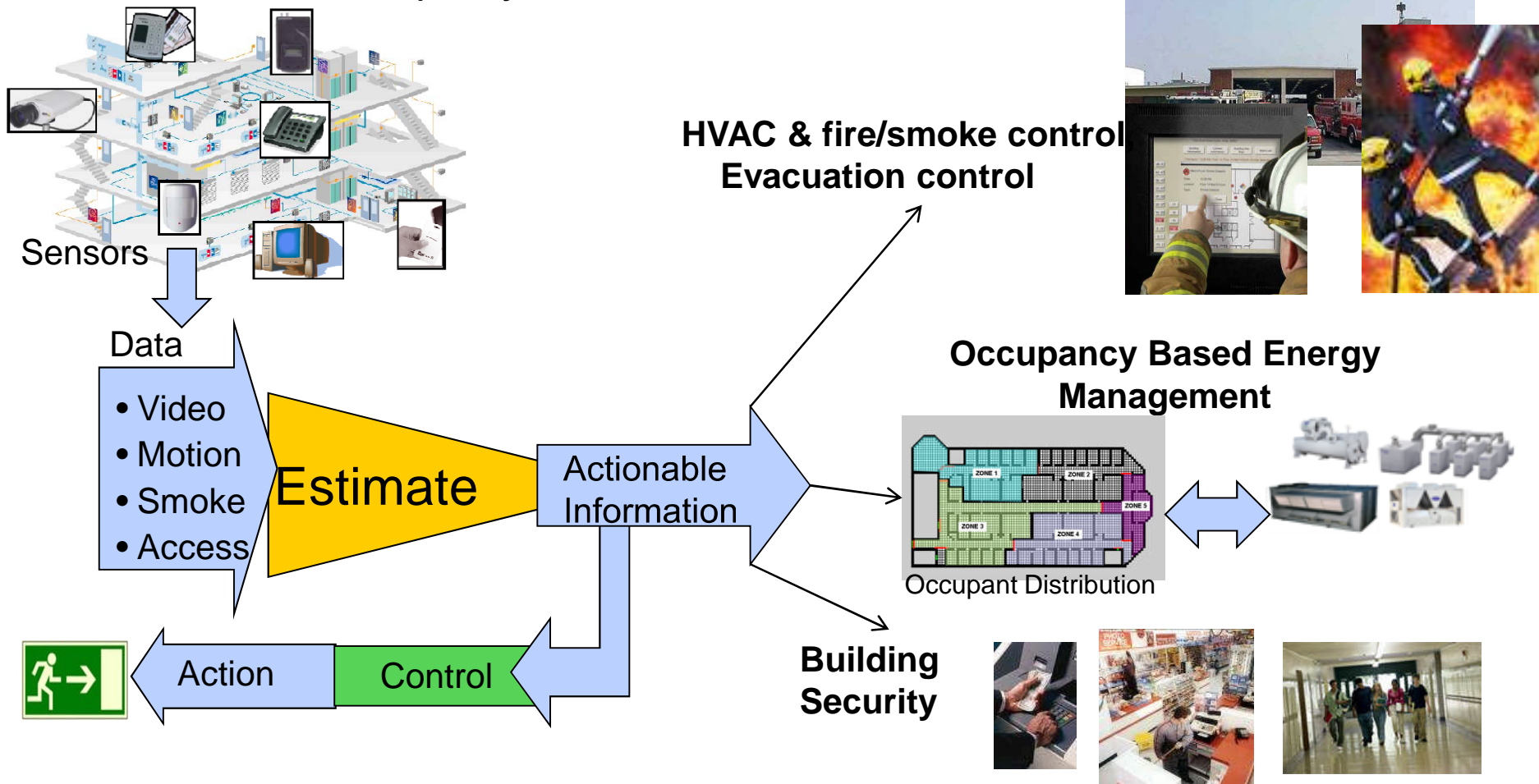
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Building Security and Energy Management

Need for real time occupancy estimation



Challenges/Barriers

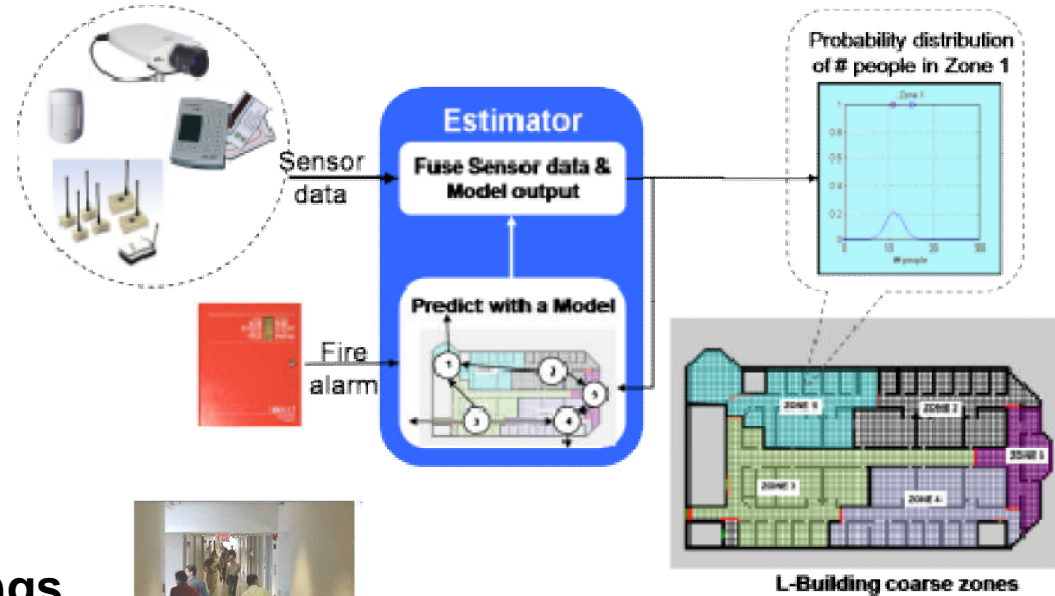
- Information volume (100's of heterogeneous sensors, 1000's of agents)
- Dynamically evolving situation (threat & response time scale overlap)
- Uncertainty (inaccurate, missing sensor data)

Enablers

- Models for occupancy
- Emerging inexpensive sensors with embedded intelligence and communication capability

Related Work: Real time Occupancy Estimation

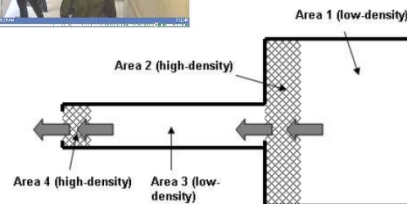
Utilizes Sensors and Models in Real-Time



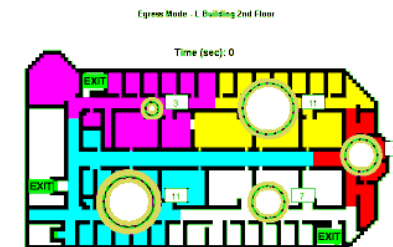
Egress in Buildings

Tomastik et al. 08 (UTRC)

- Kinetic Model for evacuation dynamics (Models vacancies in congested regions and agents in "rarified" regions)



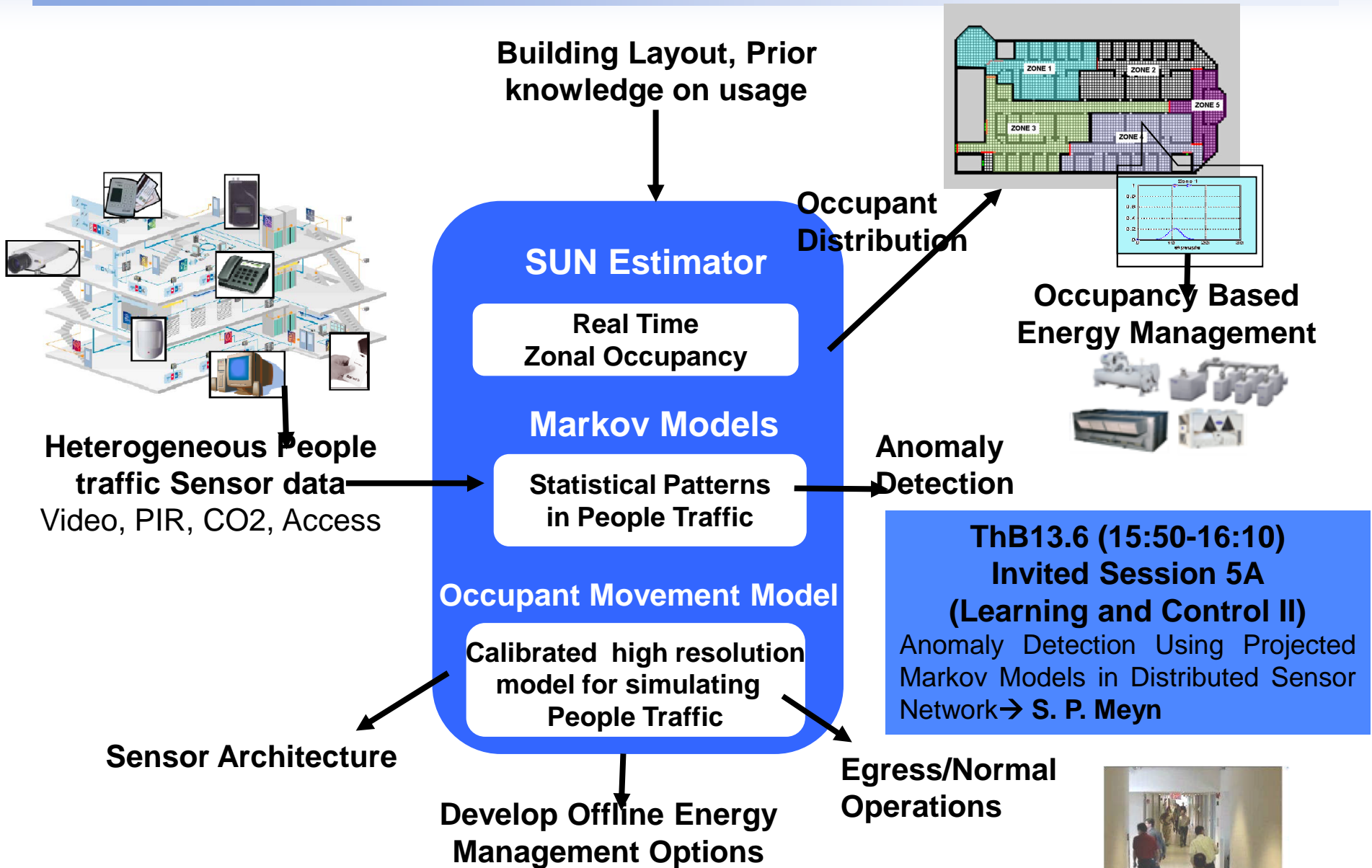
+
•Extended
Kalman
Filter



Normal Building Operation: Machine Learning Approaches, CBPD (CMU)

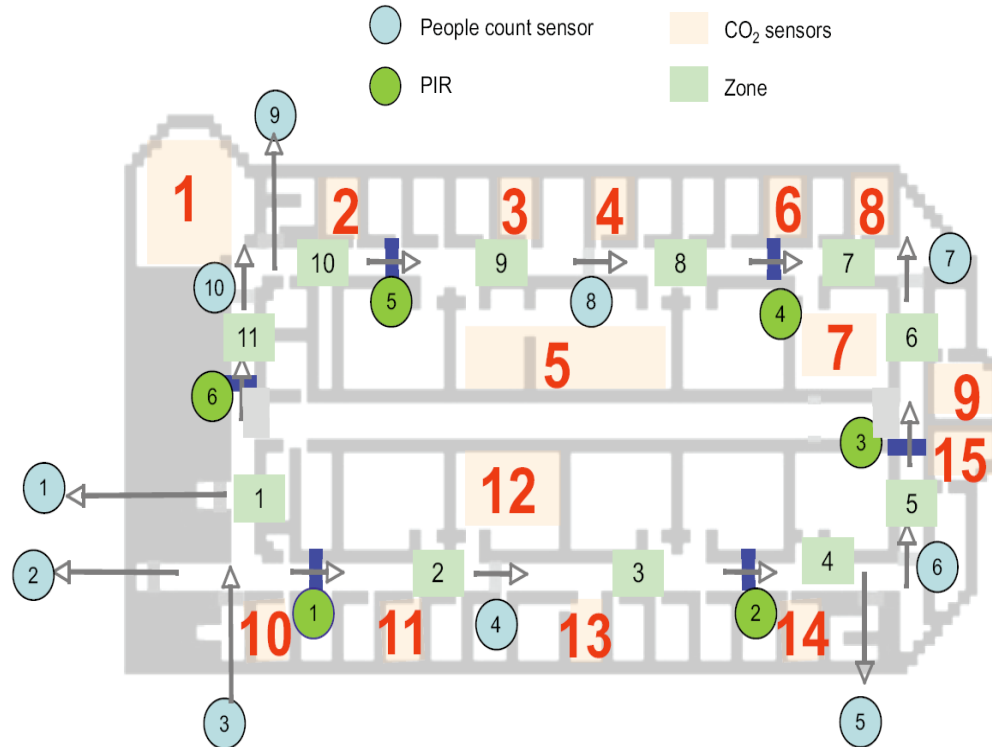
- Use of SVM, ANN, HMM (Lam et al. 09)
- Episode discovery and semi-Markov models for occupancy based ventilation control (Dong and Andrewes 09)

Occupancy Modeling Framework (UTRC)



UTRC L Building Test Bed

Video (People Count), PIR (Passive Infra Red), Co2 Sensors



Video (People Count)

Exhibit significant variance & bias:

- Overcount: Poor lighting condition (during early & late hours), Turning light switch on/off, Several crossings due to occupants loitering.
- Undercount: Multiple people crossing

PIR (Motion Detection)

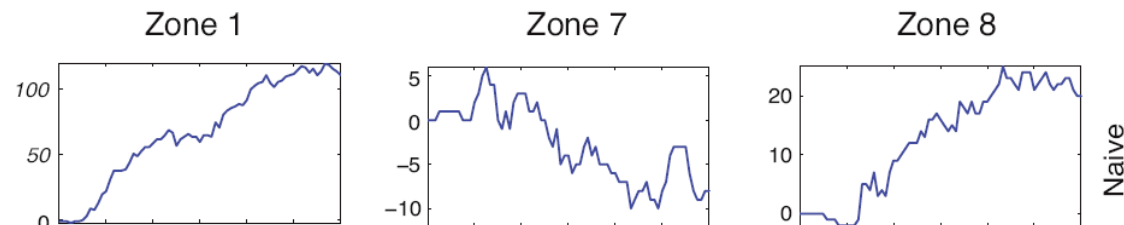
- Do not give people count information

CO₂ Sensors (Occupancy)

- High variability due to fluctuations in ambient CO₂ levels, HVAC system settings, and door open/close status
- Suffer from slow response time (about 10-20 minutes in this study)

Naive Estimator : People Count

$$\hat{x}_i(t+1) - \hat{x}_i(t) = \sum_j \hat{r}_{ji}(t) - \sum_l \hat{r}_{il}(t),$$



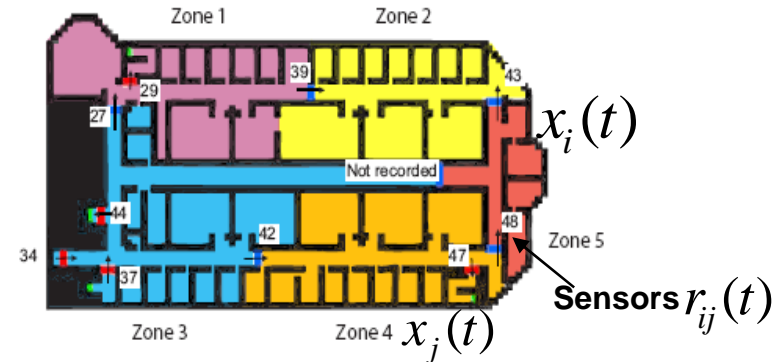
Motivation for SUN Estimation Framework

Role of Constraints and Prior Knowledge in Estimation

$$\phi(t) = \begin{pmatrix} x(t) \\ r(t) \end{pmatrix} \quad \begin{matrix} \text{Occupancy} \\ \text{Flow rate} \end{matrix}$$

$$x_i(t+1) - x_i(t) = \sum_j r_{ji}(t) - \sum_l r_{il}(t)$$

$$y(t) = C\phi(t) = \begin{bmatrix} C^x & 0 \\ 0 & C^r \end{bmatrix} \phi(t)$$



•Message from Linear Systems theory

$$\begin{aligned} \phi(t+1) &= A\phi(t) + W(t+1) \\ y(t) &= C\phi(t) + V(t+1) \end{aligned}$$

Any linear model of occupancy is not observable based on flow measurements (Rule out construction of an asymptotically stable estimator without further structure on behavior)

•Message from Statistics

$$\begin{aligned} \phi(t+1) &= f_t(\phi(t)) + W(t+1) \\ Y(t) &= h_t(\phi(t)) + V(t+1) \end{aligned}$$

MAP (Maximum a posteriori)

$$\hat{\phi}(t) = \arg \max_{\phi} p(\phi | Y_0^t)$$

Model is constrained (Gaussian assumption invalid), regardless estimation algorithm defined as an optimization, subject to state space constraints is attractive

$$-\log(p(\phi_0, \dots, \phi_T | y_0, \dots, y_{T-1})) \propto$$

$$\begin{aligned} &\|\phi_0 - \bar{\phi}_0\|_{\Sigma_0^{-1}}^2 + \sum_{t=0}^{T-1} (\|y(t) - h_t(\phi(t))\|_{\Sigma_{yt}^{-1}}^2 \\ &+ \|\phi(t+1) - f_t(\phi(t))\|_{\Sigma_{dt}^{-1}}^2) \end{aligned}$$

Information on sensor and dynamics naturally arise

SUN: Receding Horizon Estimation

SUN :Sensor, Utility & Network Structure combined through Constrained Optimization

Constrained Optimization

$$\min P_0(\phi_0) + \sum_{t=0}^T P_y(\phi(t), y(t)) + \sum_{t=0}^{T-1} P_d(\phi(t+1), \phi(t)) + \sum_{t=0}^T U_x(\phi(t))$$

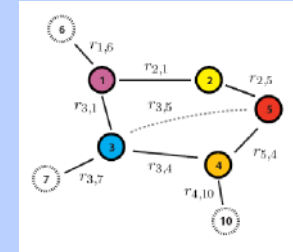
Flow Balance

$$x_i(t+1) = x_i(t) + \sum_j r_{ji}(t) - \sum_j r_{ij}(t)$$

**Bounds on Occupancy
& Flow rates**

$$XLB(t) \leq x(t) \leq XUB(t), \forall t$$

$$RLB(t) \leq r(t) \leq RUB(t), \forall t$$



**Initial state
penalty function**

$$P_0(\phi_0) = \left\| \phi_0 - \hat{\phi}_0 \right\|_{\Sigma_0^{-1}}^2$$

**Model dynamics penalty
function, e.g.: continuity**

$$P_d(\phi(t+1), \phi(t)) = \left\| x(t+1) - x(t) \right\|_{\Sigma_x^{-1}}^2 + \left\| r(t+1) - r(t) \right\|_{\Sigma_r^{-1}}^2$$

**Model and sensor
consistency
penalty function**

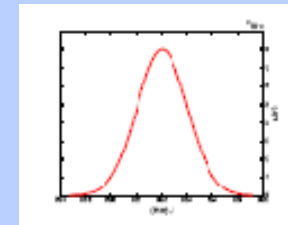
Sensor Measurements

$$P_y(\phi(t), y(t)) = \left\| r(t) - y(t) \right\|_{\Sigma_{y_t}^{-1}}^2$$

**Occupancy Utility
Function**

$$U_x(x(t)) = \left\| x(t) - m(t) \right\|_{\Sigma_{xt}^{-1}}^2$$

Prior Knowledge



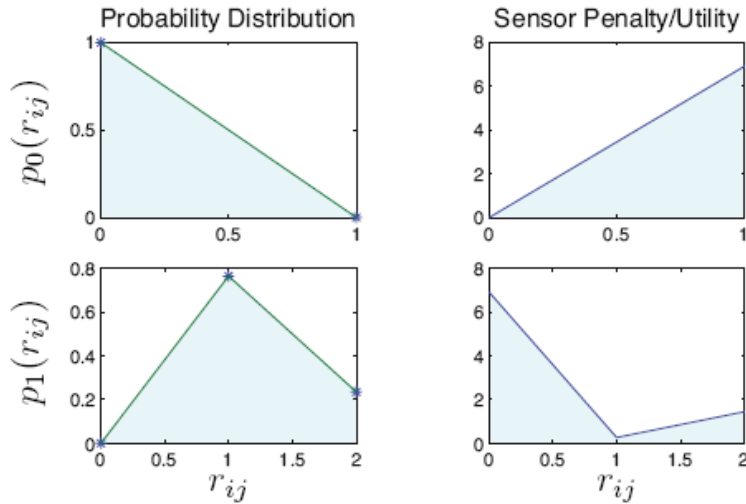
- Building space usage pattern
- Preferences for walking speed, proximity, path
- Clustering, Lane formation
- Behavior dependence on age, mobility, aggressiveness...

Soft Sensor Penalty for Video and PIR Sensors

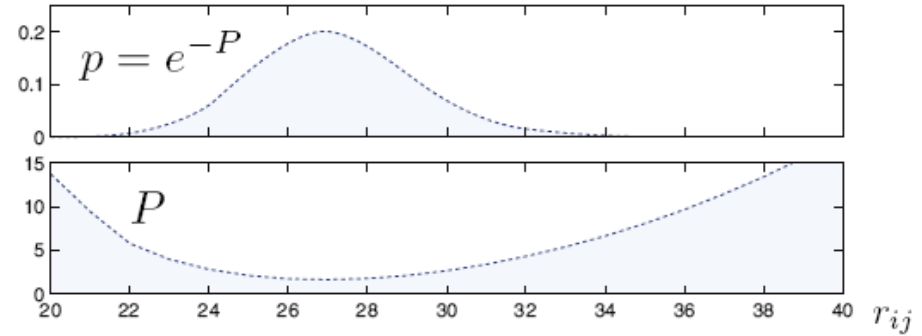
Composed (in time) sensor utility admits a quadratic approximation

Soft Penalty /Utility for Sensor

$$p_i(r) = e^{-P_i(r)}$$



Composition of Soft Penalty



Quadratic Soft Penalty

$$\mathcal{P}_y(\phi, y) = \sum_{i=1}^{N_f} \sum_{j>i} P_{y_{ij}}$$

$$P_{y_{ij}}(r_{ij}, y_{ij}) = \frac{1}{2}(y_{ij} - b_{ij}(y_{ij}))^2 / \sigma_{ij}^2$$

Bias **Variance**



Y_{ij}	8am < t < 5pm	$t < 8\text{am}$ or $t > 5\text{pm}$
0	$b_{ij} = 0, \quad \sigma_{ij}^2 = 10^{-5}$	$b_{ij} = 0, \quad \sigma_{ij}^2 = 10^{-5}$
1	$b_{ij} = 0, \quad \sigma_{ij}^2 = 0.5$	$b_{ij} = 0, \quad \sigma_{ij}^2 = 1$
2	$b_{ij} = -0.25, \quad \sigma_{ij}^2 = 1.2$	$b_{ij} = -1, \quad \sigma_{ij}^2 = 2.4$
> 3	$b_{ij} + Y_{ij} = 1, \quad \sigma_{ij}^2 = 2$	$b_{ij} + Y_{ij} = 1, \quad \sigma_{ij}^2 = 4.5$

Table 1
Soft penalty/utility parameters for People Count Sensors



Y_{ij}	8am < t < 5pm	$t < 8\text{am}$ or $t > 5\text{pm}$
0	$b_{ij} = 0, \quad \sigma_{ij}^2 = 10^{-2}$	$b_{ij} = 0, \quad \sigma_{ij}^2 = 10^{-4}$
1	$b_{ij} = 0, \quad \sigma_{ij}^2 = 100$	$b_{ij} = 0, \quad \sigma_{ij}^2 = 1$

Table 2
Soft penalty/utility parameters for PIR Sensors

Occupancy Utility via Smoothing

Smoothing using historical data

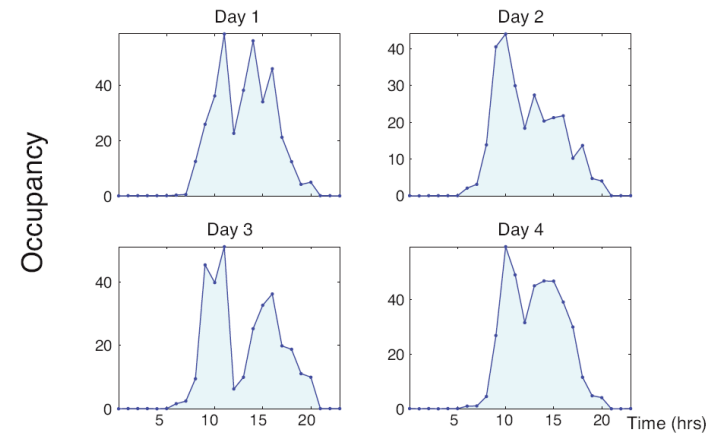
SUN for whole day
enforcing zero occupancy at
boundaries & using Sensor Utility
(hourly time scale)

$$\mu_i = N^{-1} \sum_{k=1}^N \hat{x}_i^k, \quad \sigma_i^2 = N^{-1} \sum_{k=1}^N (\hat{x}_i^k - \mu_i)^2$$

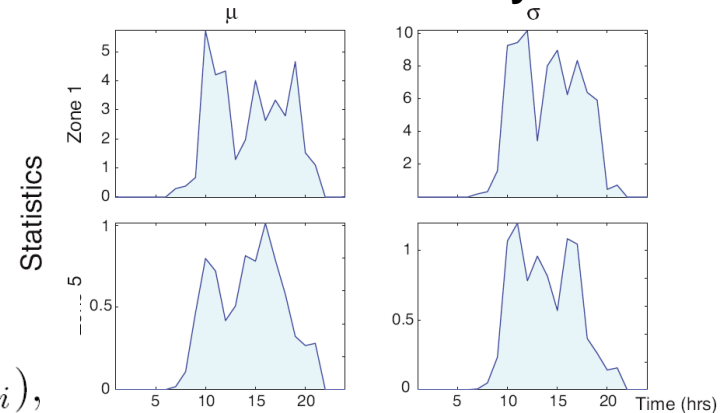
$k = 1, \dots, N$ Days

$$\mathcal{U}_i(x_i) = -\frac{1}{2}(x_i - \mu_i)^2 / \sigma_i^2$$

Occupancy Utility $\mathcal{U}_x(x) = \sum_{i=1}^{N_z} \mathcal{U}_i(x_i),$



Based on 16 Days



Prediction

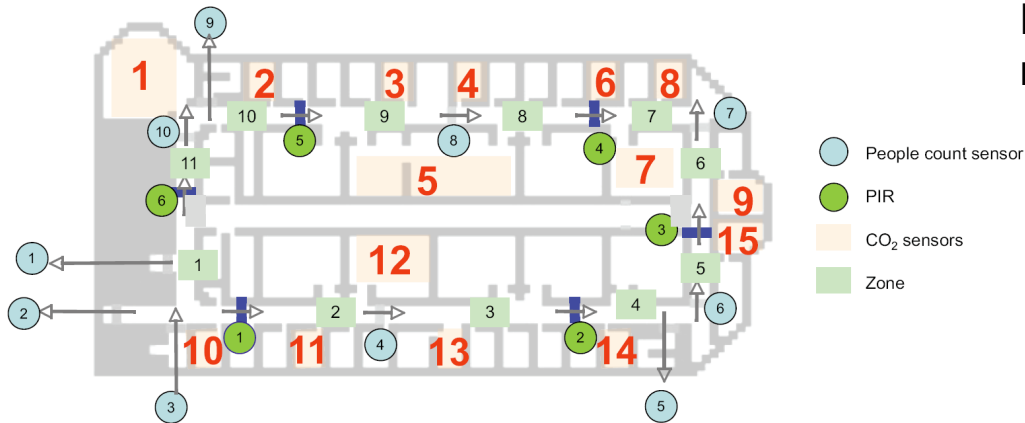
$$\arg \min_{\phi_T, \dots, \phi_{T_1}} \left\{ \sum_{t=T}^{T_1-1} (\mathcal{P}_d(\phi(t+1), \phi(t)) - \mathcal{U}_x(\phi(t))) \right\}$$

Smoothing & Prediction

$$\arg \min_{\phi_0, \dots, \phi_T, \dots, \phi_{T_1}} [\mathcal{P}_{\text{smooth}} + \mathcal{P}_{\text{predict}}]$$

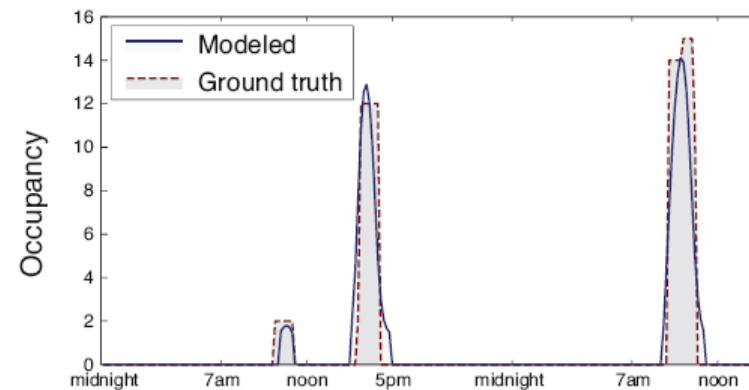
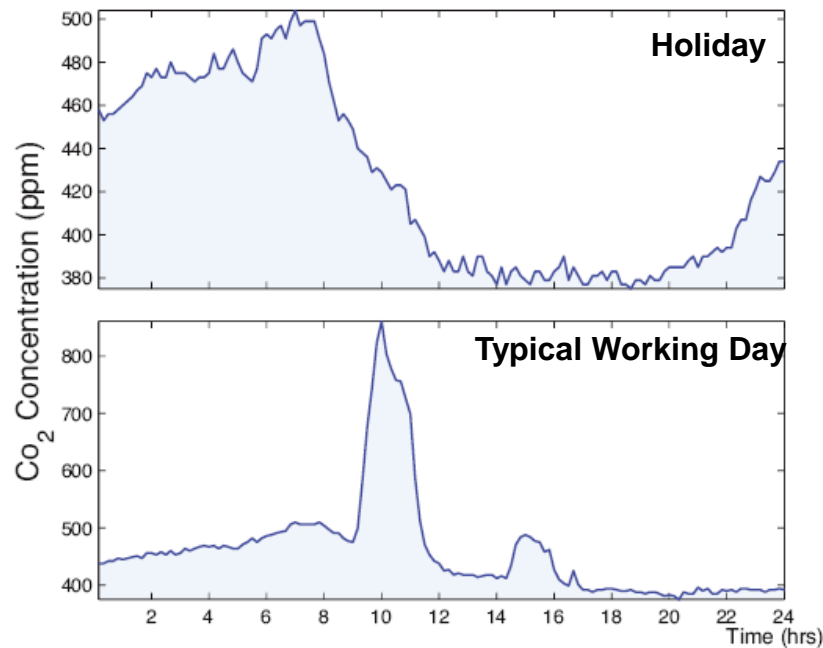
C0₂ Utility

Follow smoothing procedure (like for occupancy) to obtain C0₂ Utility



Reformulation to account for partial C0₂ measurement in each zone

$$\phi(t) = \begin{pmatrix} x(t) \\ x^c(t) \\ r(t) \end{pmatrix} \quad \hat{x}_i(t+1) + \sum_{j=1}^{N_{ci}} \hat{x}_j^c(t+1) = \hat{x}_i(t) + \sum_{j=1}^{N_{ci}} \hat{x}_j^c(t) + \sum_j \hat{r}_{ji}(t) - \sum_l \hat{r}_{il}(t),$$

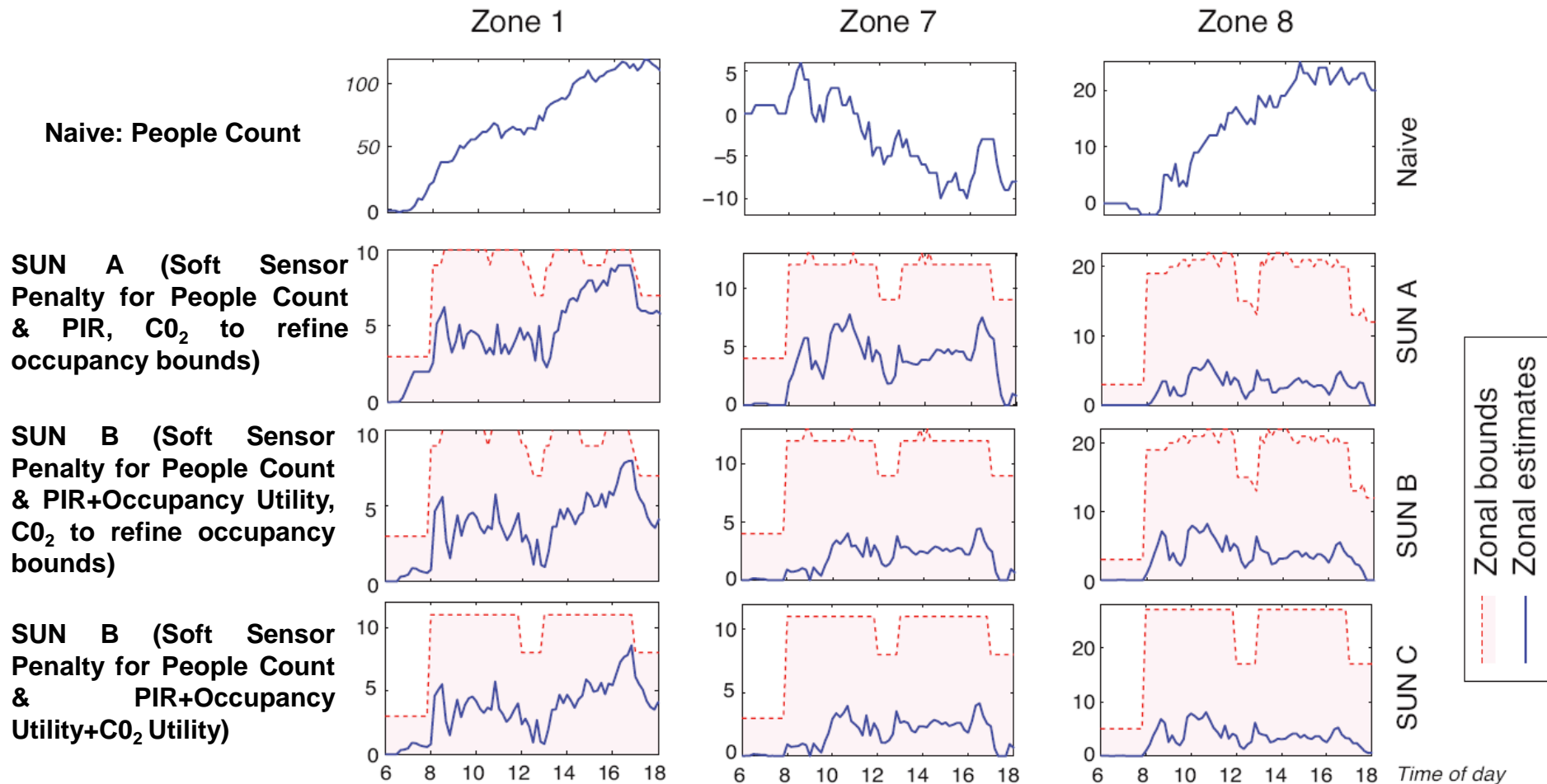


$$y_i(t+1) = \alpha y_i(t) + \beta \hat{x}_i^c(t),$$

C0₂ Data Occupancy

Occupancy Estimation using SUN

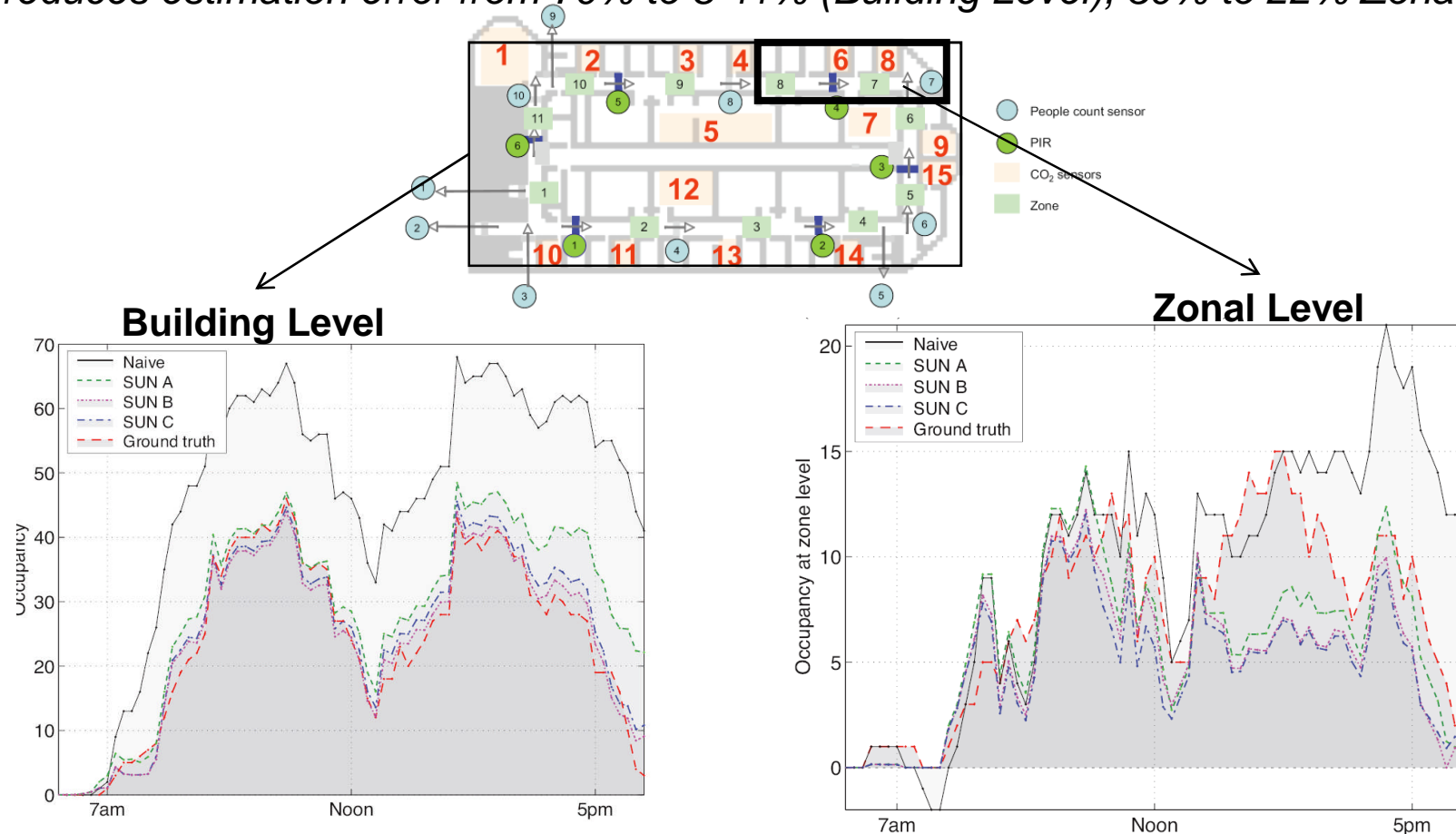
Assessing impact of different sources of information



**Zonal Bounds Based on
Typical Room Usage Pattern**

Summary : Occupancy Estimation Error

SUN reduces estimation error from 70% to 8-11% (Building Level), 30% to 22% Zonal Level



Ground Truth: Manually by sifting through video data 6pm

$$E = \frac{1}{T_f - T_0} \sum_{t=T_0, x(t) \neq 0}^{T_f} \frac{|x(t) - \hat{x}(t)|}{x(t)},$$

	Building Level Error	Zonal Level Error
Naive	70%	30%
SUN A	21%	20%
SUN B	8%	21%
SUN C	11%	22%

Conclusions

Contributions:

SUN (Sensor-Utility-Network)

- Occupancy estimation via solution of a receding-horizon convex optimization problem
- Gives a systematic framework for suitably combining inputs from distributed sensor measurements (e.g. video, PIR, access & CO₂), along with historical data regarding building utilization in estimation
- Demonstrated feasibility and superior performance of SUN in a Test Bed

Current Research:

- Evaluation of performance of SUN estimator in predictive applications (e.g. for occupancy based ventilation control)
- Adaptive techniques for learning building usage and associated utility functions
- Sensitivity of utility functions for spaces and buildings of similar type
- Optimal sensor architecture (numbers, types and locations) for SUN performance/cost tradeoff.
- Decentralized SUN